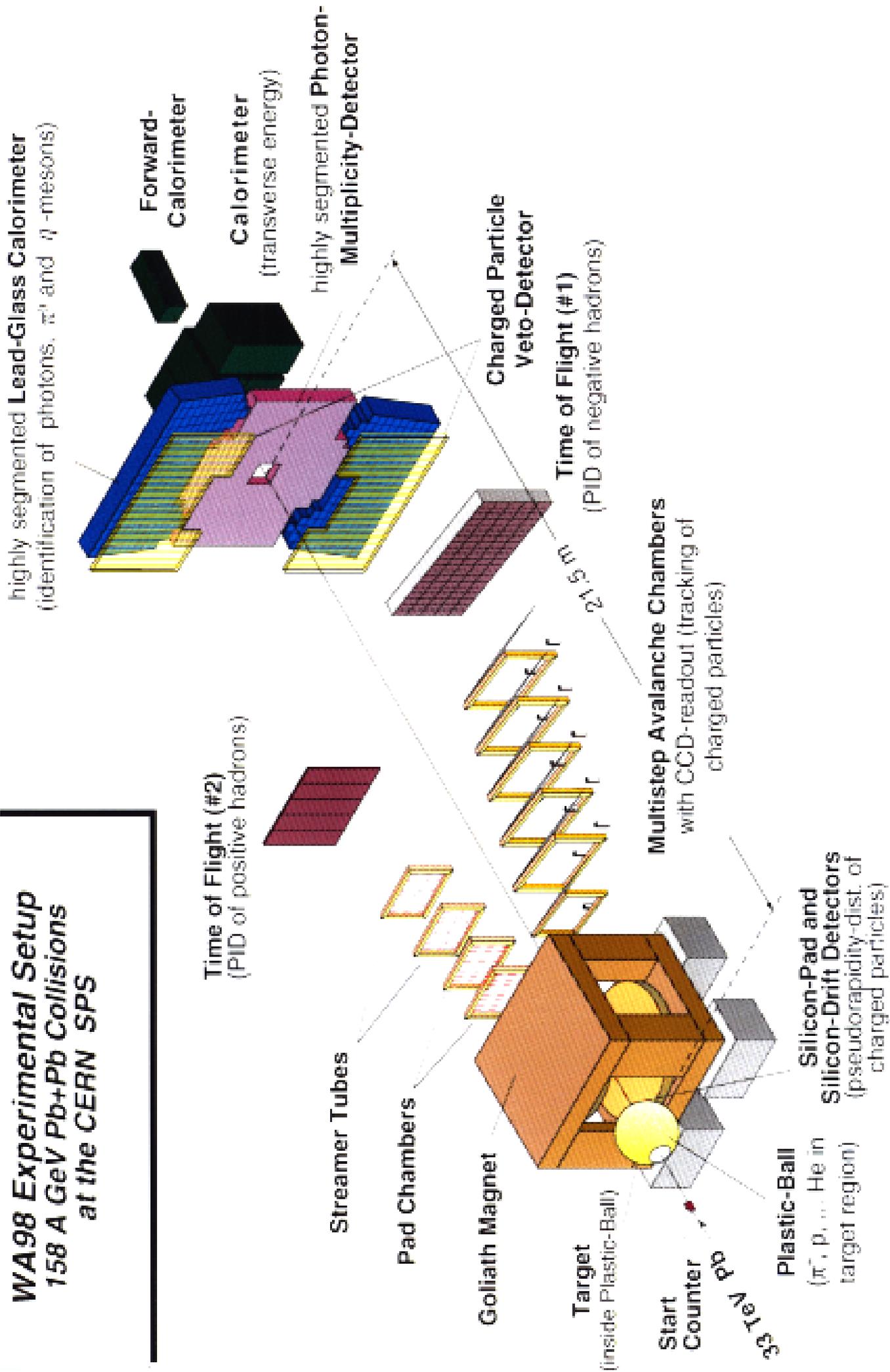


One-, Two- and Three-Particle  
Distributions from Central Pb+Pb  
Collisions at  $158A \text{ GeV}/c$



Laurent Rosselet for the WA98 Collaboration

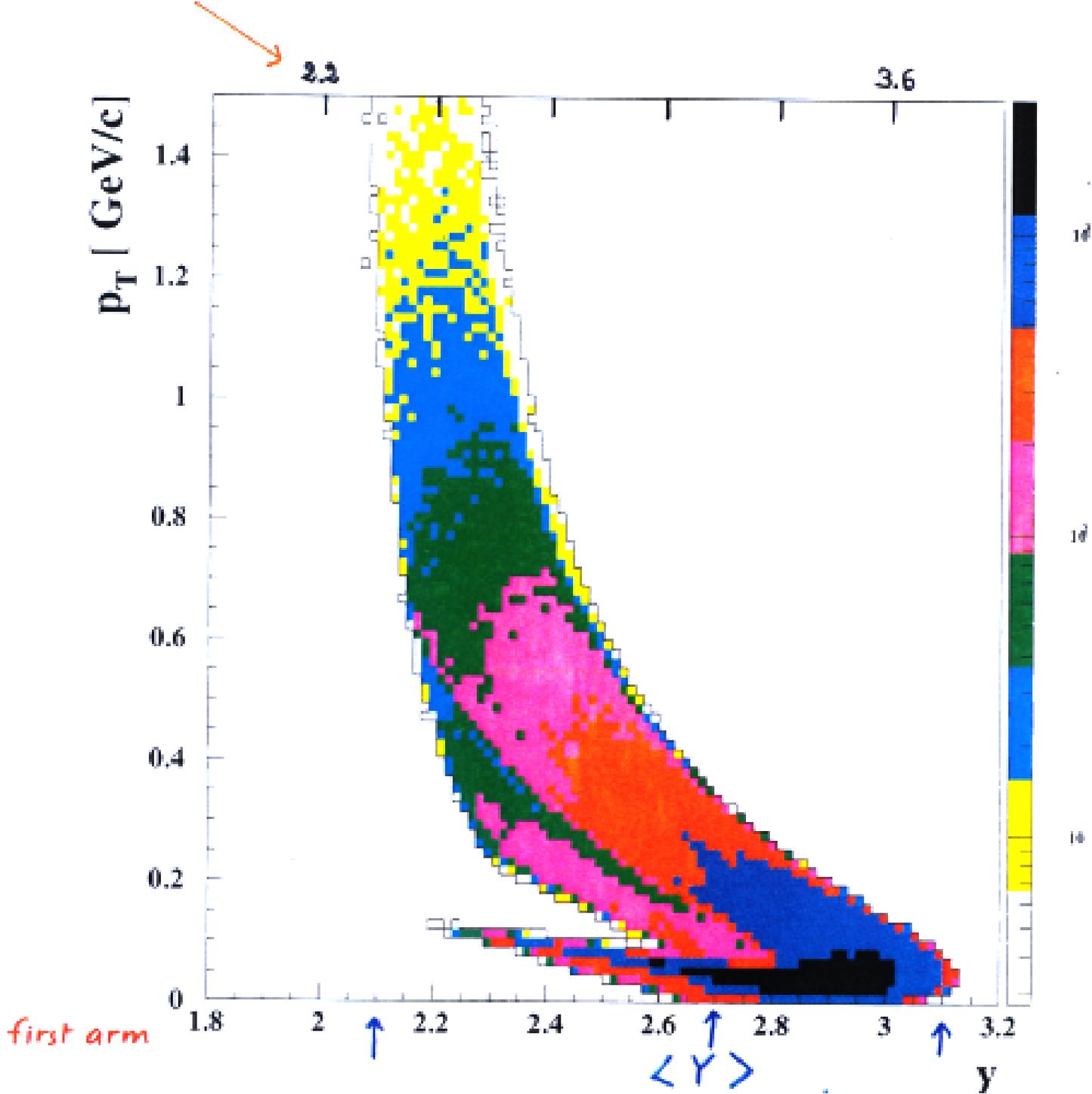
# WA98 Experimental Setup 158 A GeV Pb+Pb Collisions at the CERN SPS



$p_T$  - rapidity acceptance for  $\pi$

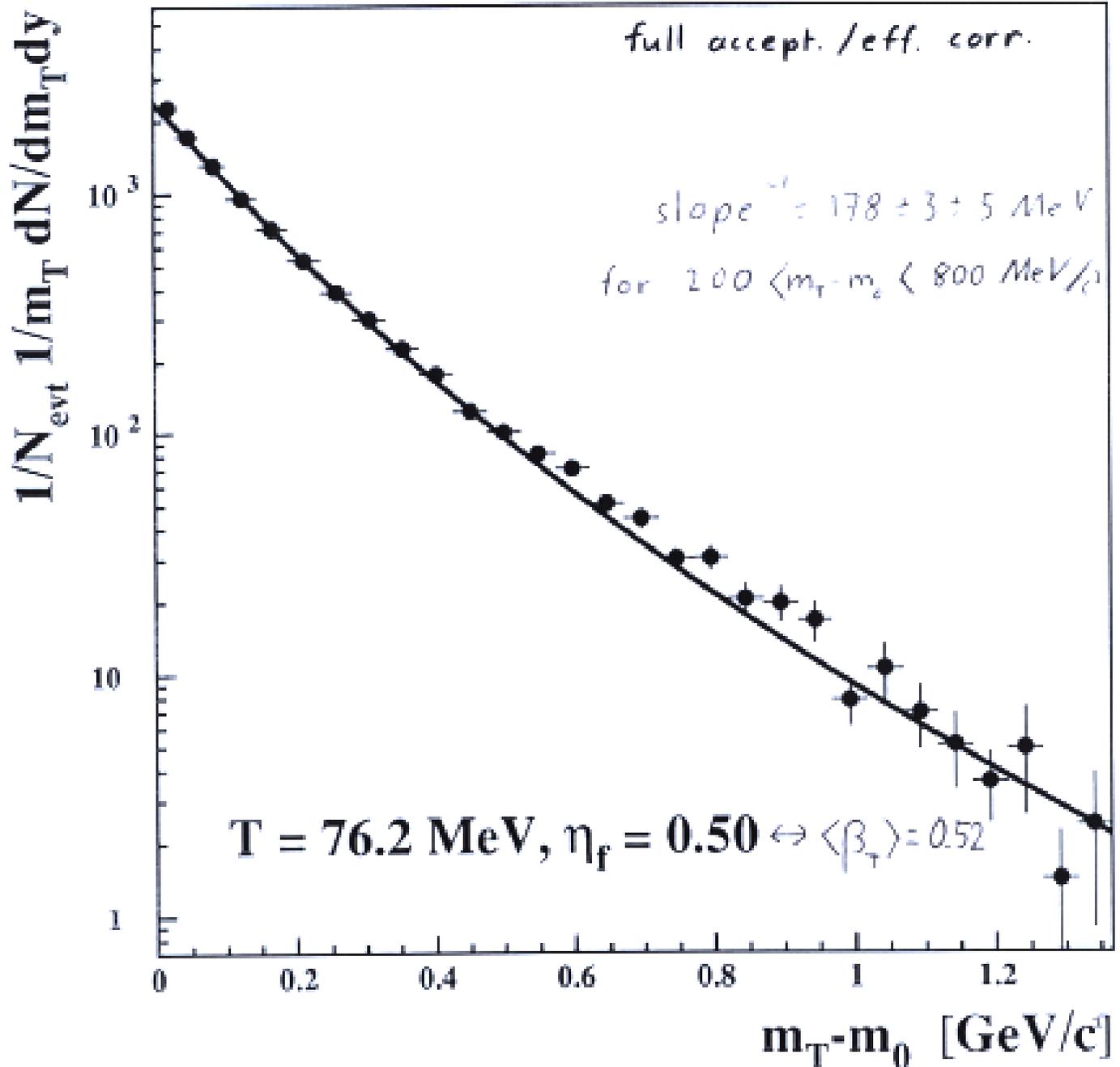
identified by T. a. F. (resol. 120ps and 90ps.

scale for 2<sup>nd</sup> arm

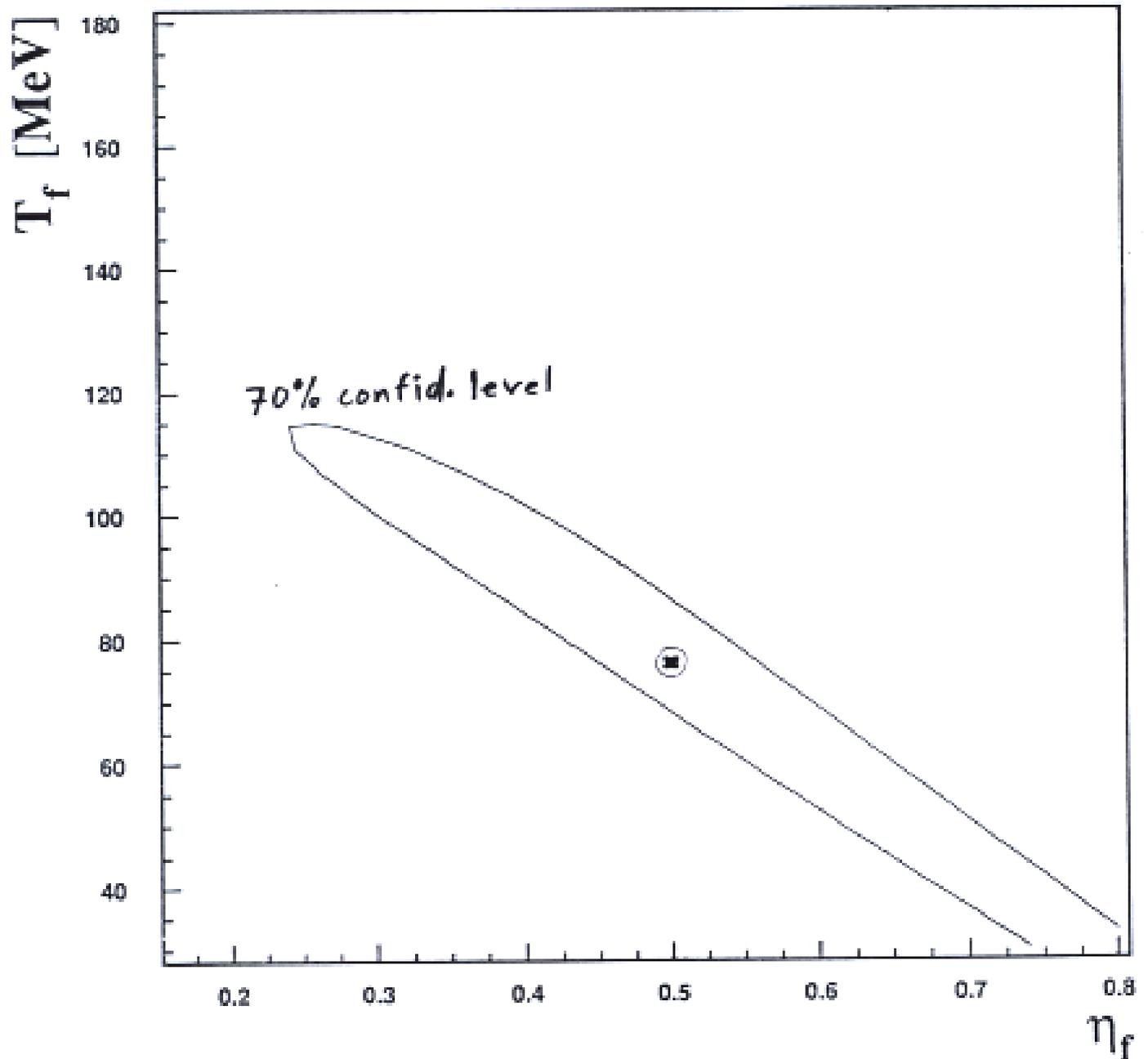


$\pi^-$  central triggers firstarm  
half of data

full accept. / eff. corr.



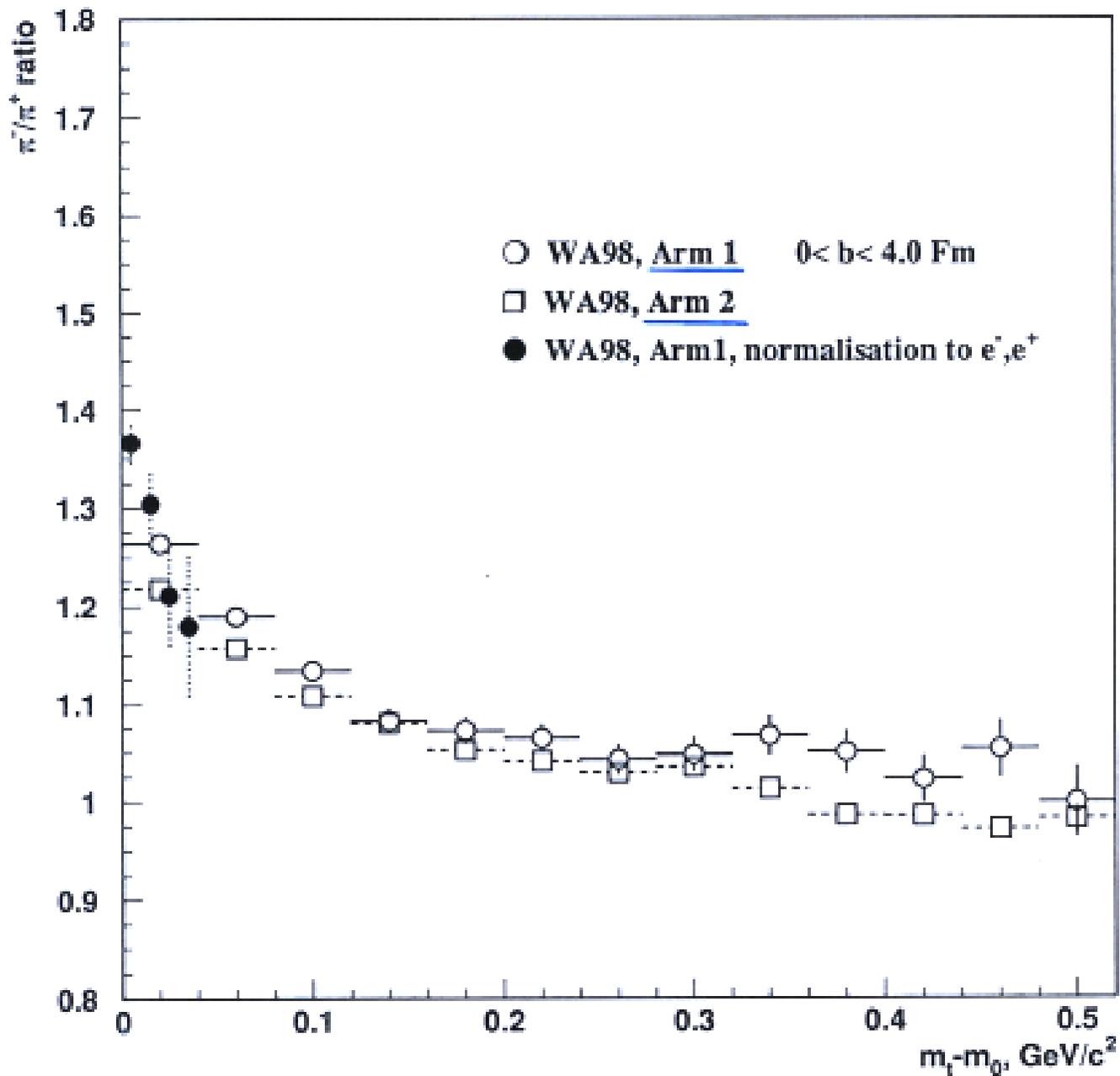
J. A. Wiedemann and U. Heinz, Phys. Rev. C 56, 3265 (1997)



Similar  $m_T$  distribution for  $\Pi^-$  and  $\Pi^+$ .

∴ extraction of  $T_f$  is delicate

$\pi^-/\pi^+$  ratio:

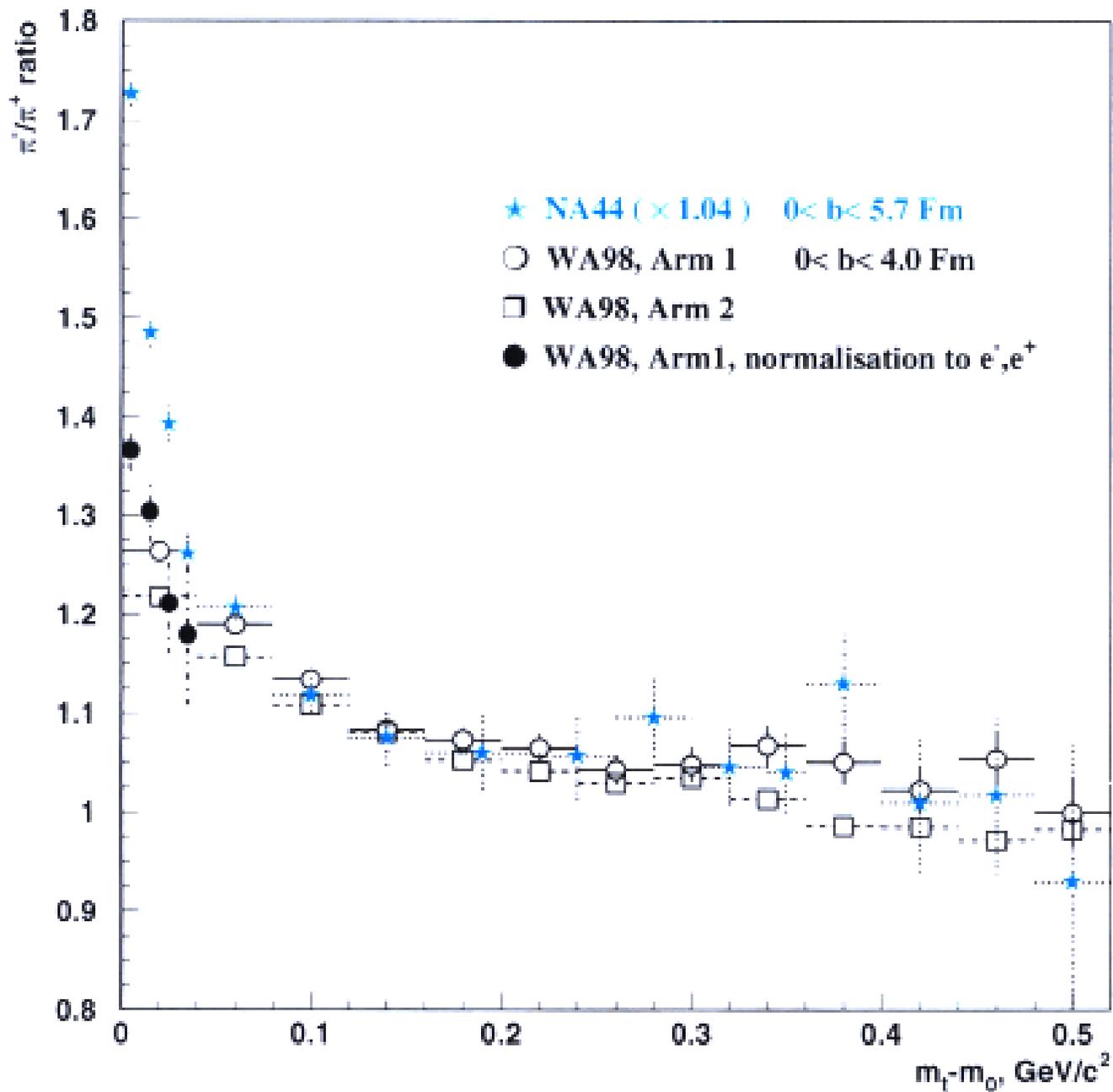


each arm is treated as a separate exp.

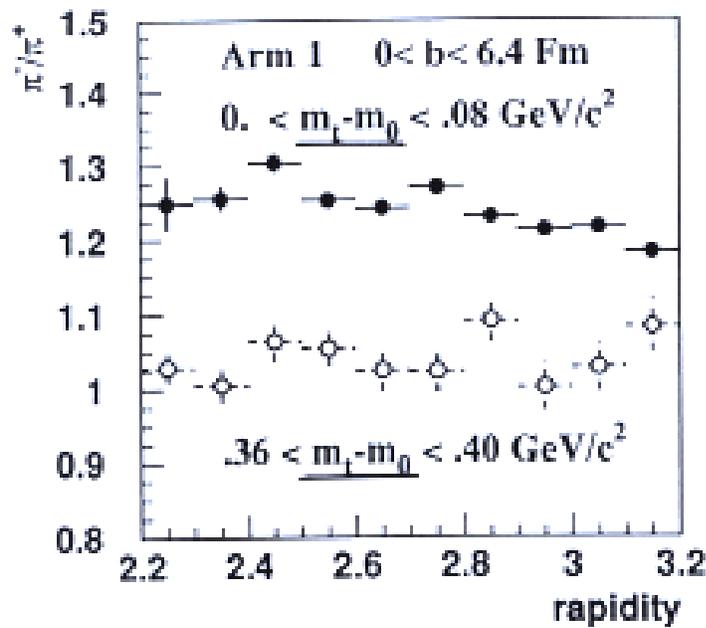
using normal and reverse field ...

..

excess at small  $m_f$

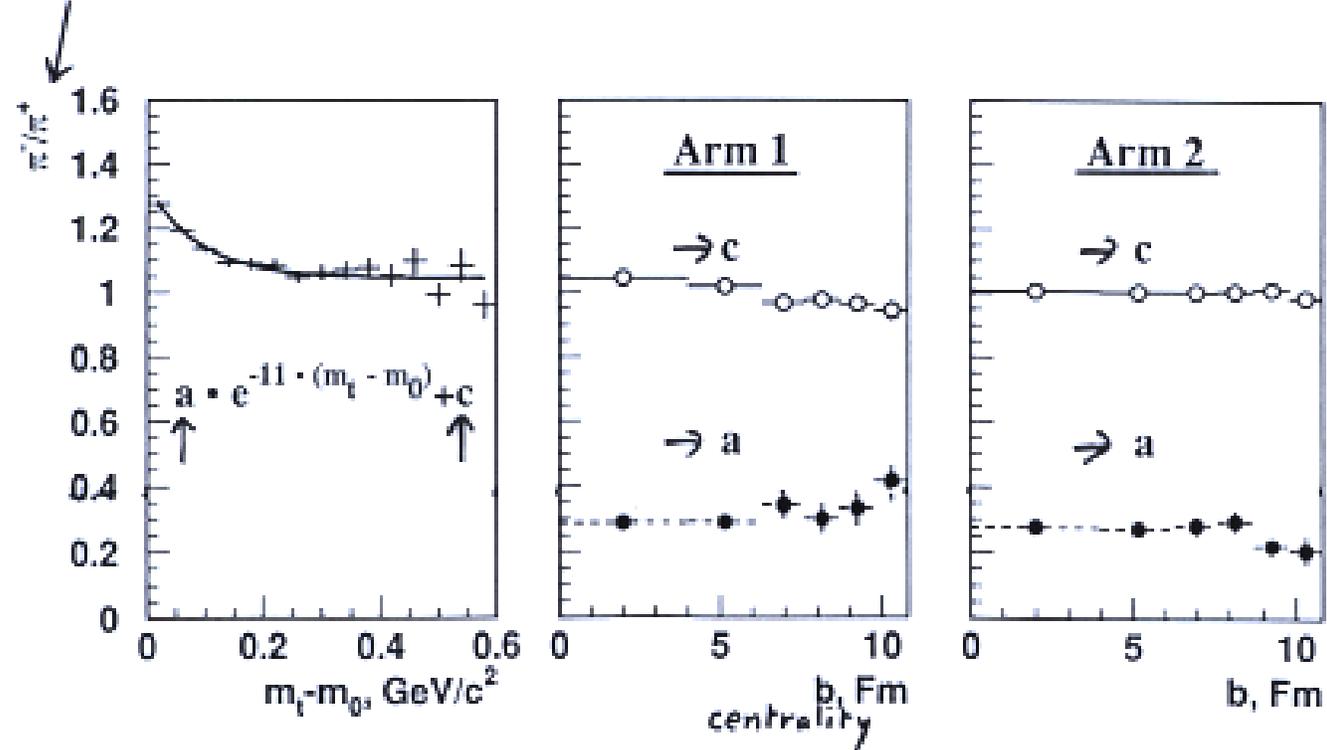


excess smaller than measured by NA44



⇒ ratio cte within acceptance range

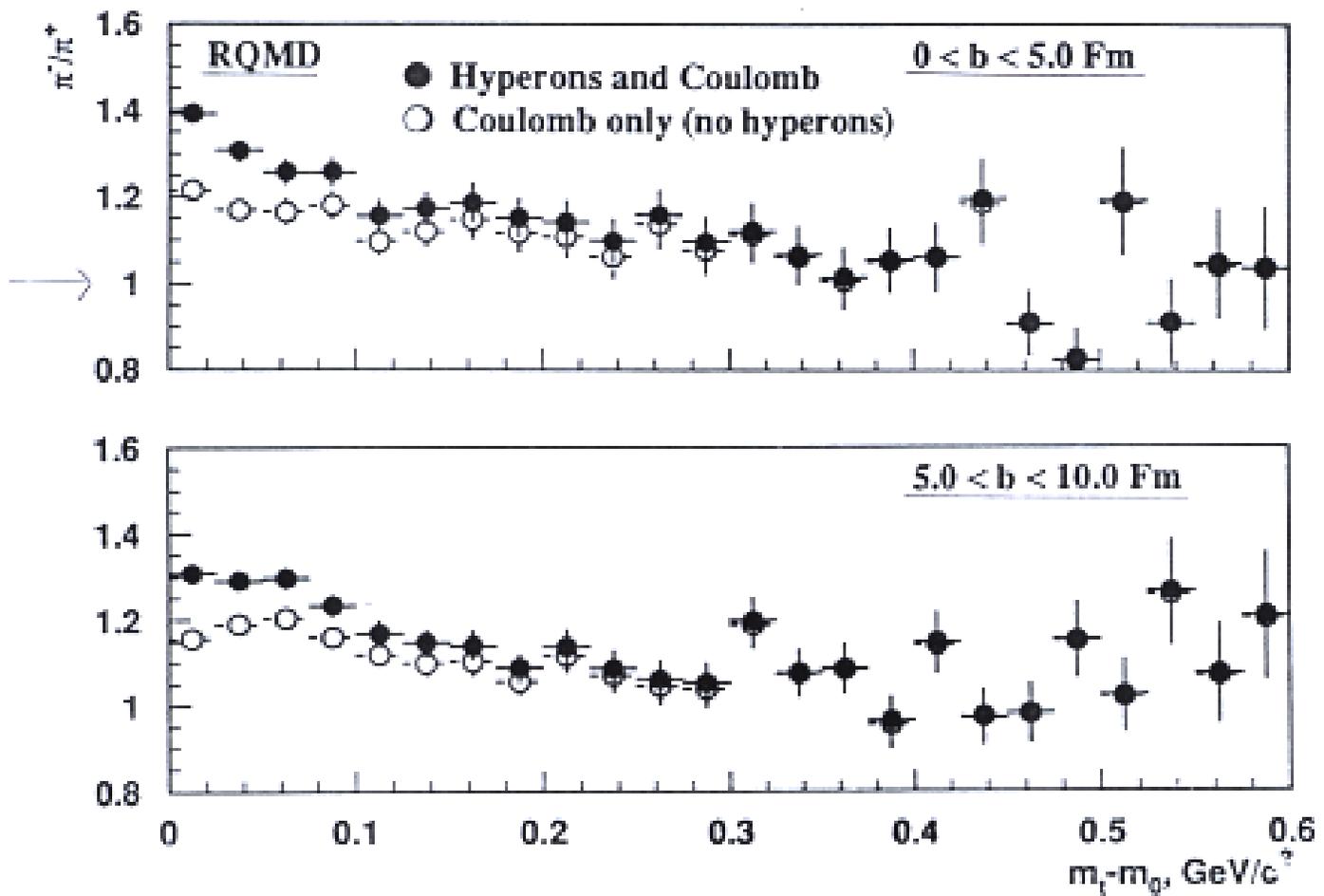
fit to



⇒ ratio cte for  $b < 10$  fm

no data for  $b > 10$  fm

Monte-Carlo study

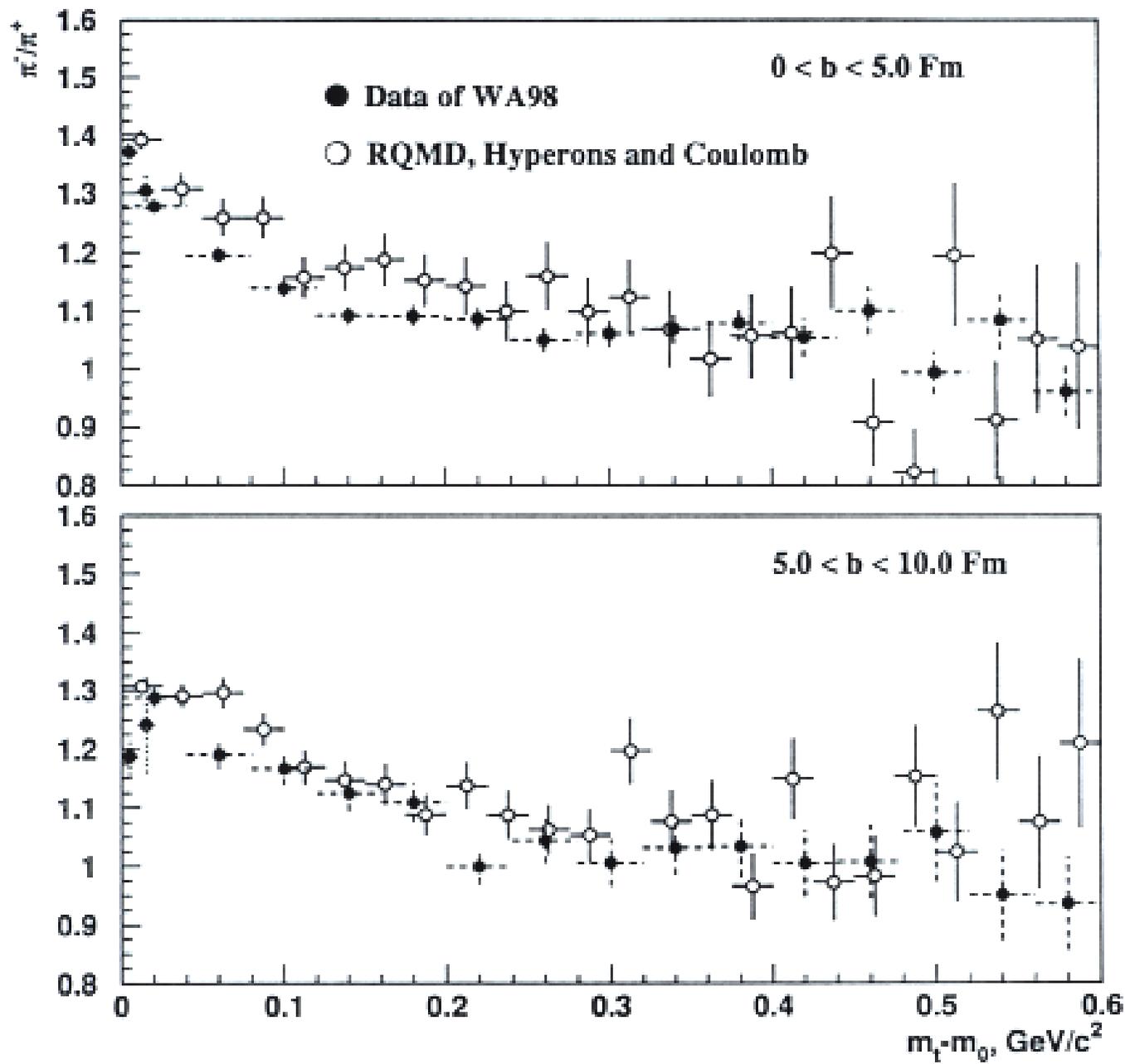


∴ half effect

Coulomb

half effect

hyp. decays

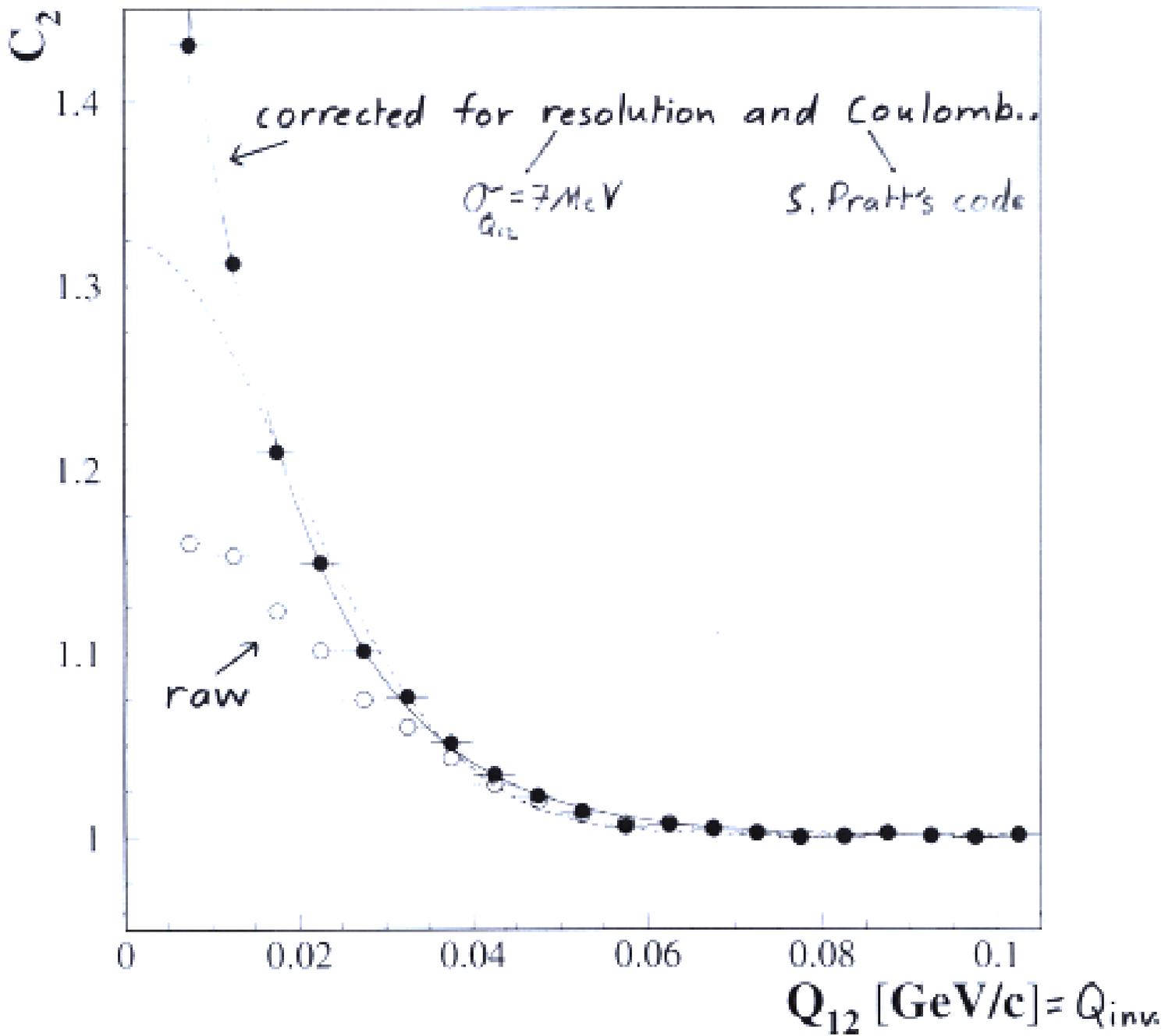


$\Pi^- \Pi^-$  correlation

Central triggers: 10% of min. bias cross section

$13.7 \times 10^6$  pairs

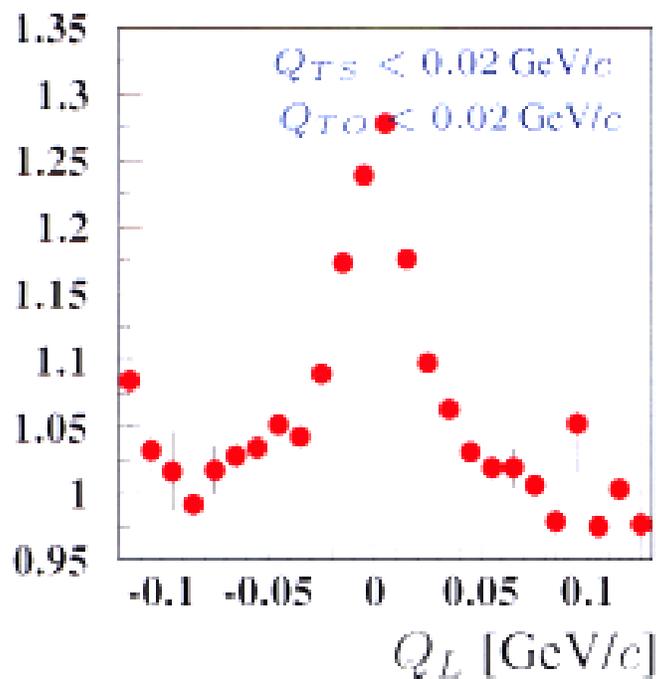
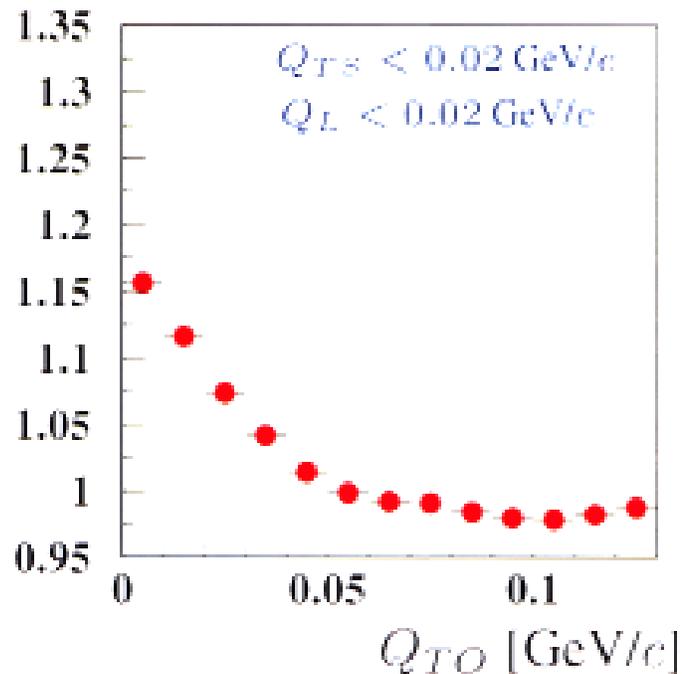
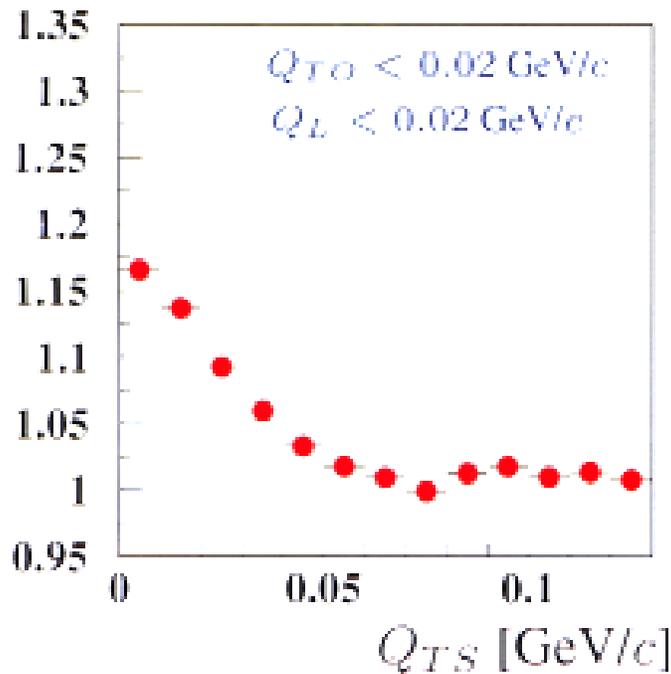
full data set...



Clearly exponential  $C_2 = 1 + \lambda e^{-2 Q_{inv} R}$  with  $R = 7.33 \pm 0.08 \text{ fm}$   
 $\lambda = 0.789 \pm 0.009$

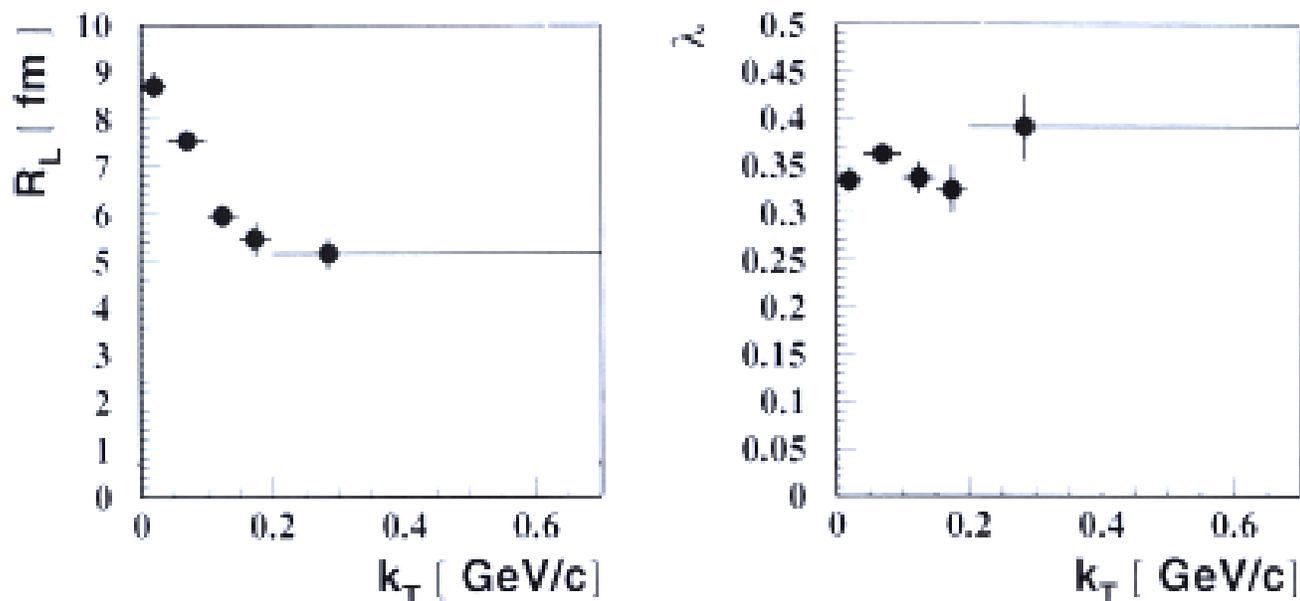
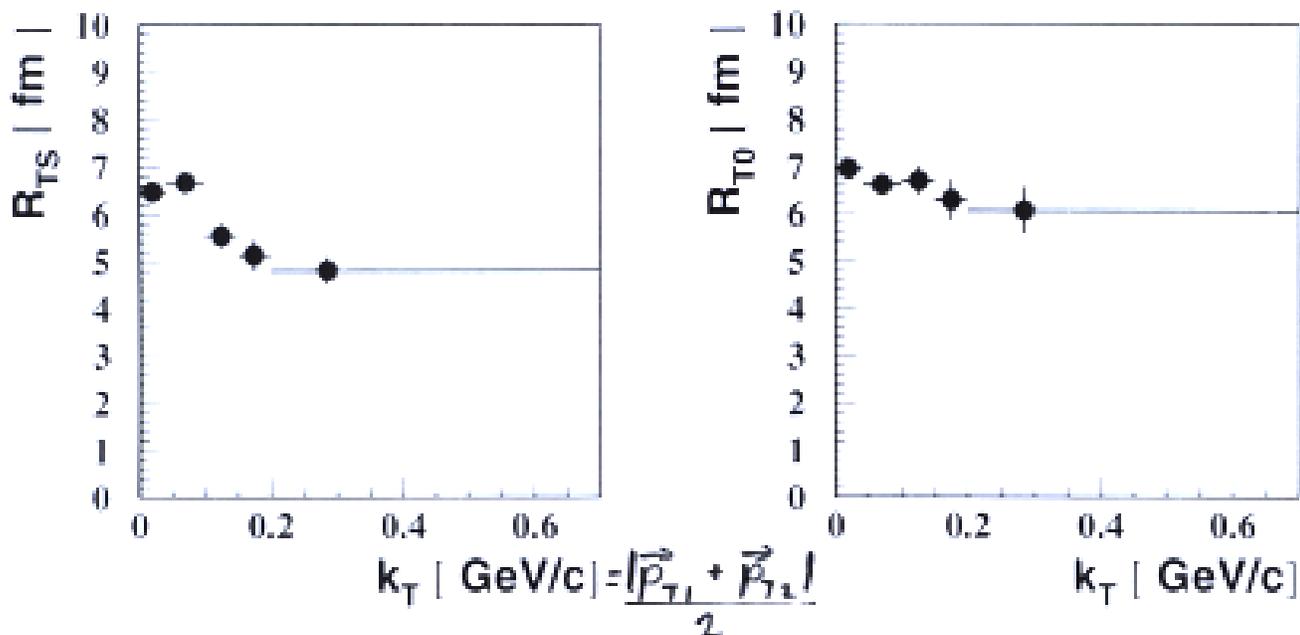
...

# Slice distributions for the $Q_{TS}$ , $Q_{TO}$ and $Q_L$ variables



# Pratt-Bertsch parameterization in the LCMS

fit includes cross-term

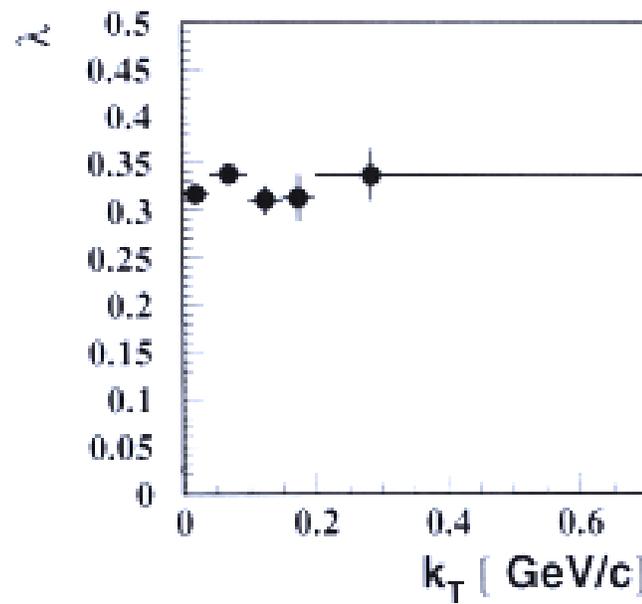
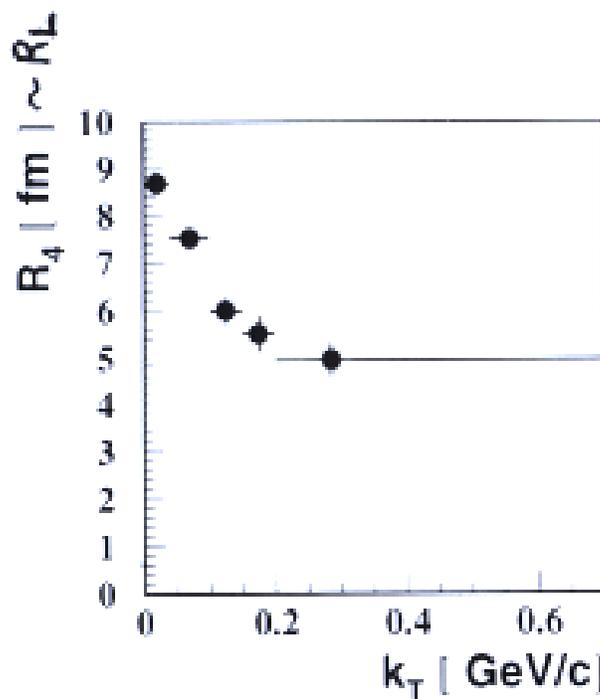
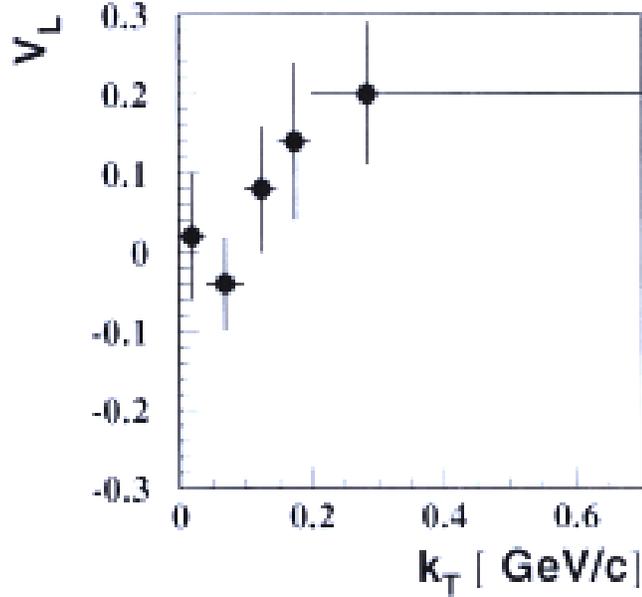
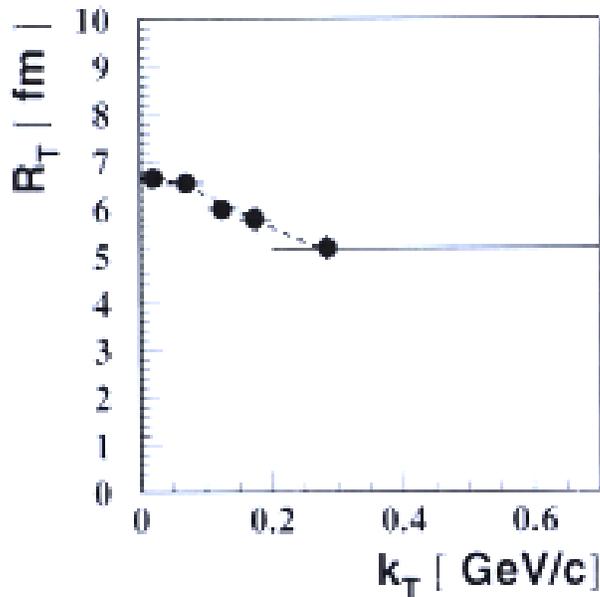


... transverse flow < longitudinal flow

# Yano-Koonin parameterization

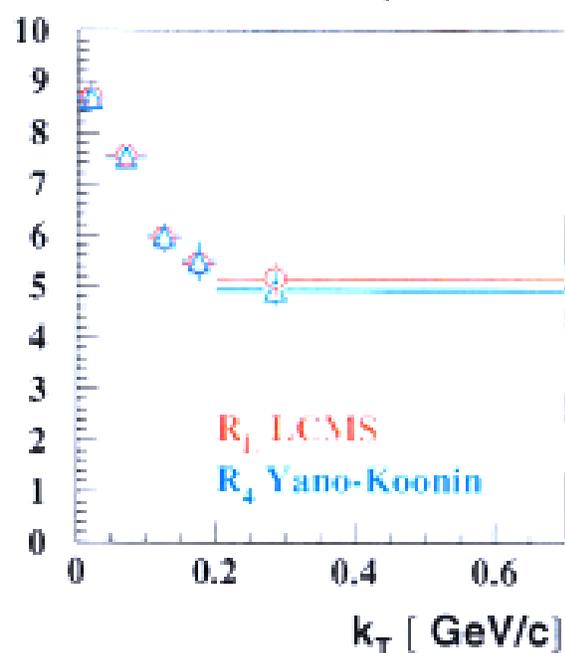
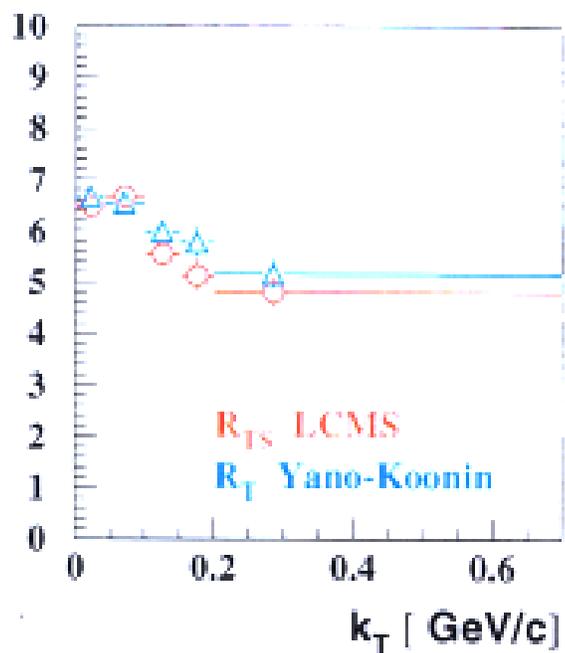
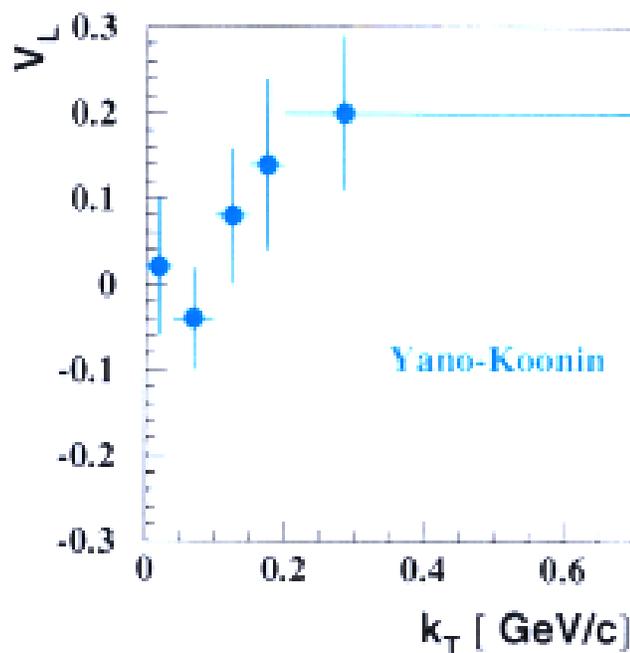
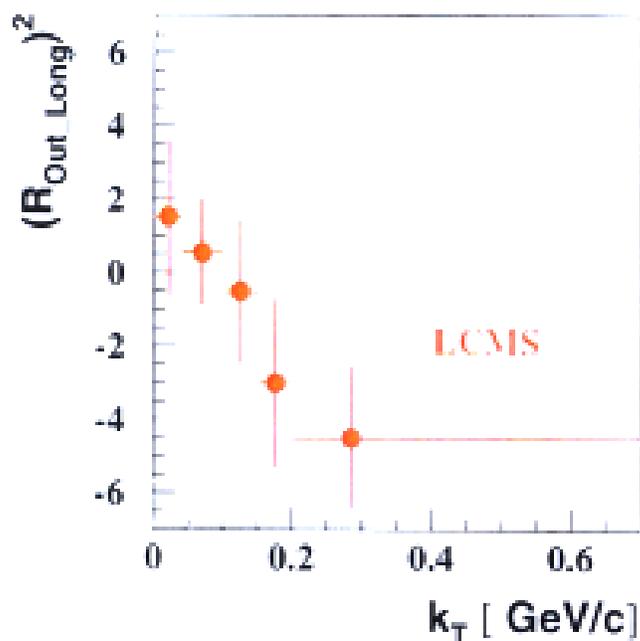
connects  $\Upsilon$ - $k$  frame to LCMS ...

$\Rightarrow$  not fully boost invar.



...  $R_0 \sim \Delta \uparrow \sim 0$  at all  $k_T$   
 ↑  
 duration of emission

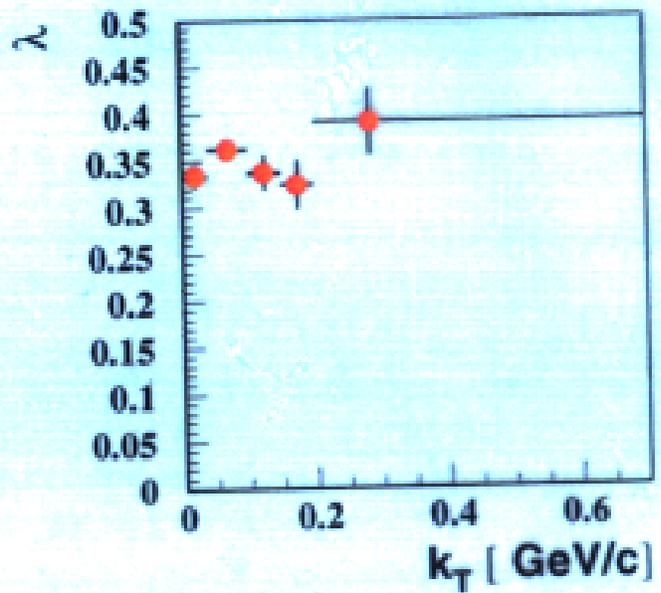
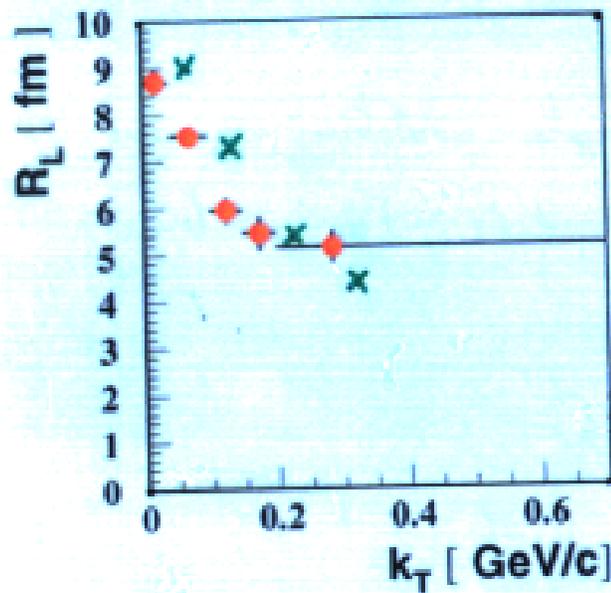
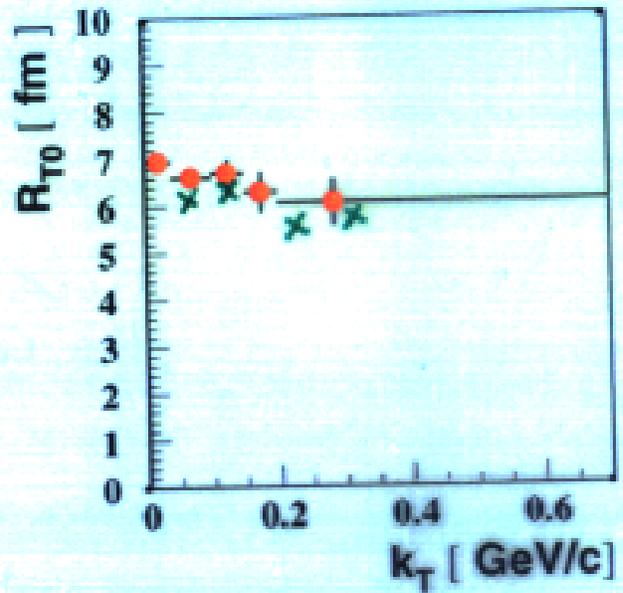
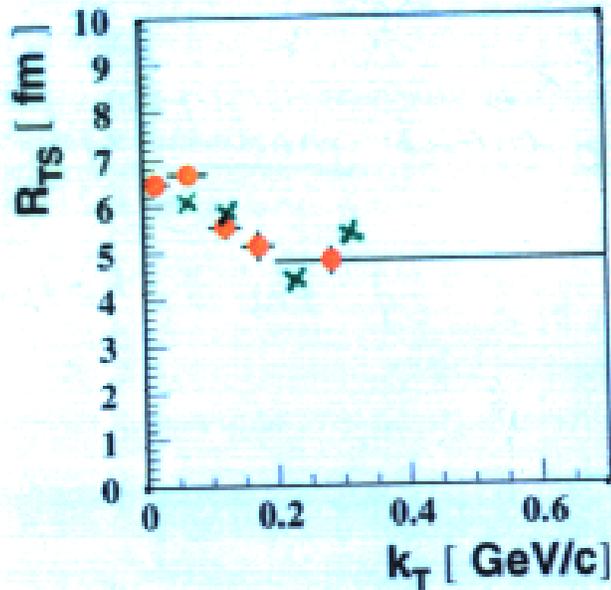
Comparison Pratt-Bertsch and Yano-Koonin param.

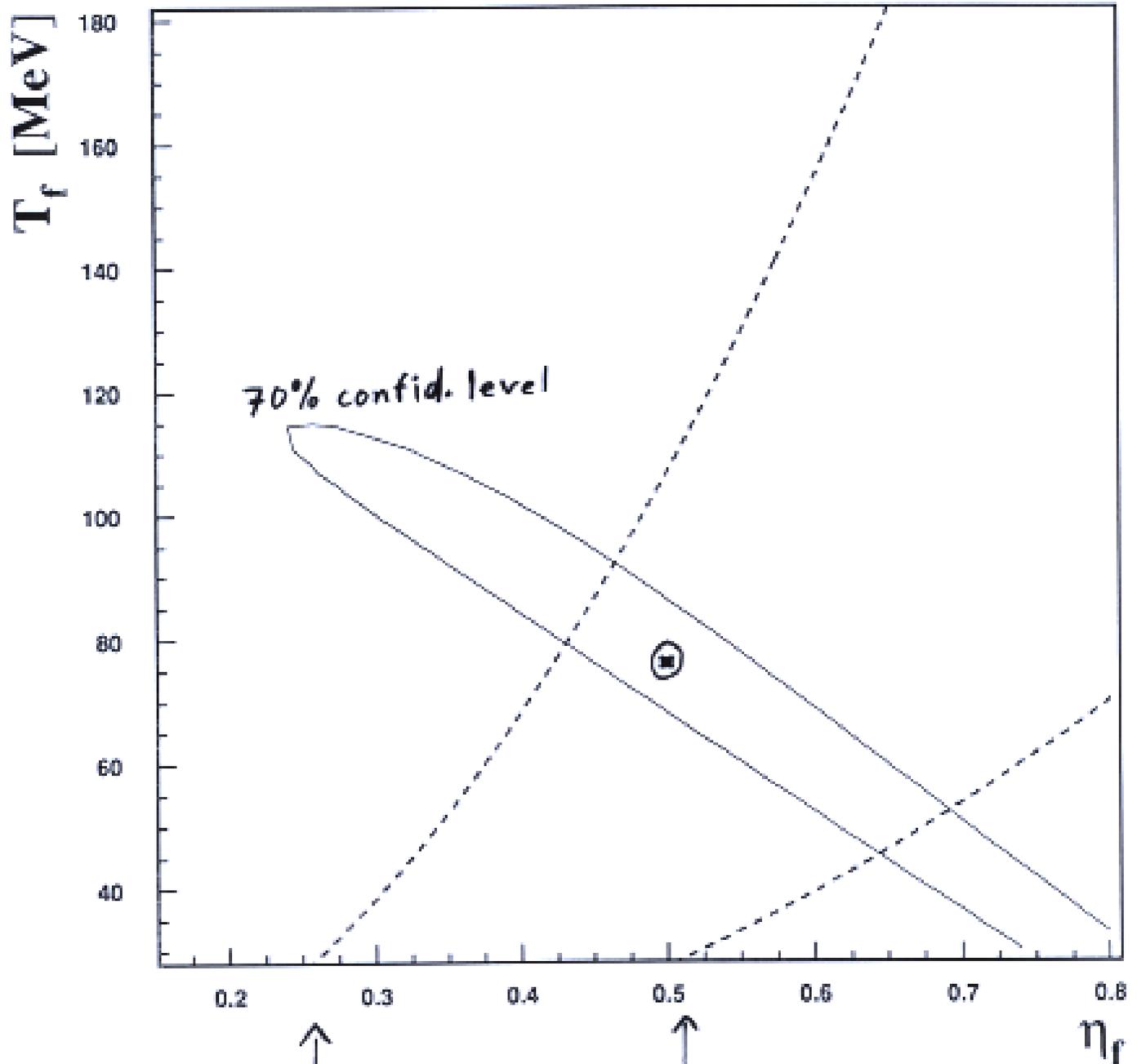


good agreement

WA98  $\pi^- \pi^-$  with  $\langle Y_{\pi^- \pi^-} \rangle = 2.70$

NA49  $h^- h^-$  with  $\langle Y_{h^- h^-} \rangle = 3.2$





$\pm 1 \sigma$  HBT constraint from fit  $R_T = R_0 \left[ 1 + m_T \cdot \frac{\eta_f^2}{T_f} \right]^{-1/2}$

from WA98 - some data

with  $m_T = \sqrt{m_\pi^2 + k_T^2}$

• • •

### 3 identical boson correlation:

if source fully chaotic:  $C_2 = 1 + |F_{12}|^2$

$$C_3 = 1 + |F_{12}|^2 + |F_{23}|^2 + |F_{31}|^2 + 2 \operatorname{Re} \{ F_{12} F_{23} F_{31} \}$$

genuine 3-body correlation

with  $F_{ij} \equiv |F_{ij}| e^{i\phi_{ij}}$ :

and  $W = \cos(\phi_{12} + \phi_{23} + \phi_{31})$

$$2 |F_{12}| |F_{23}| |F_{31}| \cdot W$$

$$|W| < 1$$

$$< 2 |F_{12}| |F_{23}| |F_{31}|$$

$$\text{with } Q_3^2 \equiv Q_{12}^2 + Q_{23}^2 + Q_{31}^2: \quad 2 \lambda^{3/2} e^{-R^2 Q_3^2 / 2} \quad \text{or} \quad 2 \lambda^{3/2} e^{-R(Q_{12} + Q_{23} + Q_{31})}$$

Gaussian  $C_2$

expon.  $C_2$

$R$  obtained by  $C_2 \Rightarrow$  access to the phase  $W$  of F.T. of source function  
{ asymmetry of the source  
if  $W=1 \Leftrightarrow$  F.T. real  $\Leftrightarrow$  symmetrical

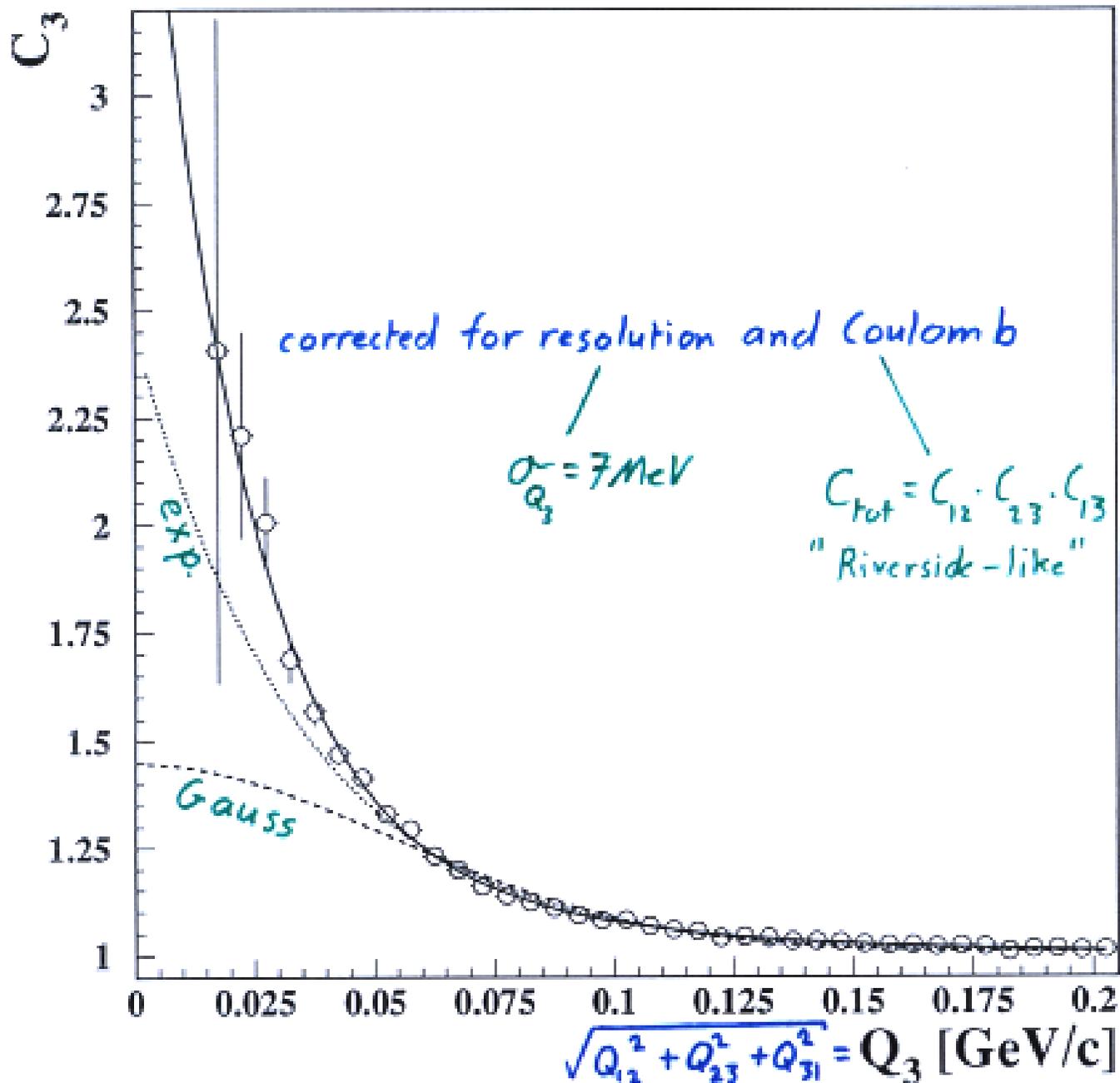
• • •

If source not fully chaotic,  $W$  is the strength of true 3-body correlation  
if  $W \neq 1 \Leftrightarrow$  coherency



# $\pi^- \pi^- \pi^-$ correlation

central triggers  
 $8.2 \times 10^6$  triplets



$$C_3 = 1 + \lambda_1 \exp[-2 Q_3 R_1] + \lambda_2 \exp[-2 Q_3 R_2]$$

$$R_1 = 5.01 \pm 0.38$$

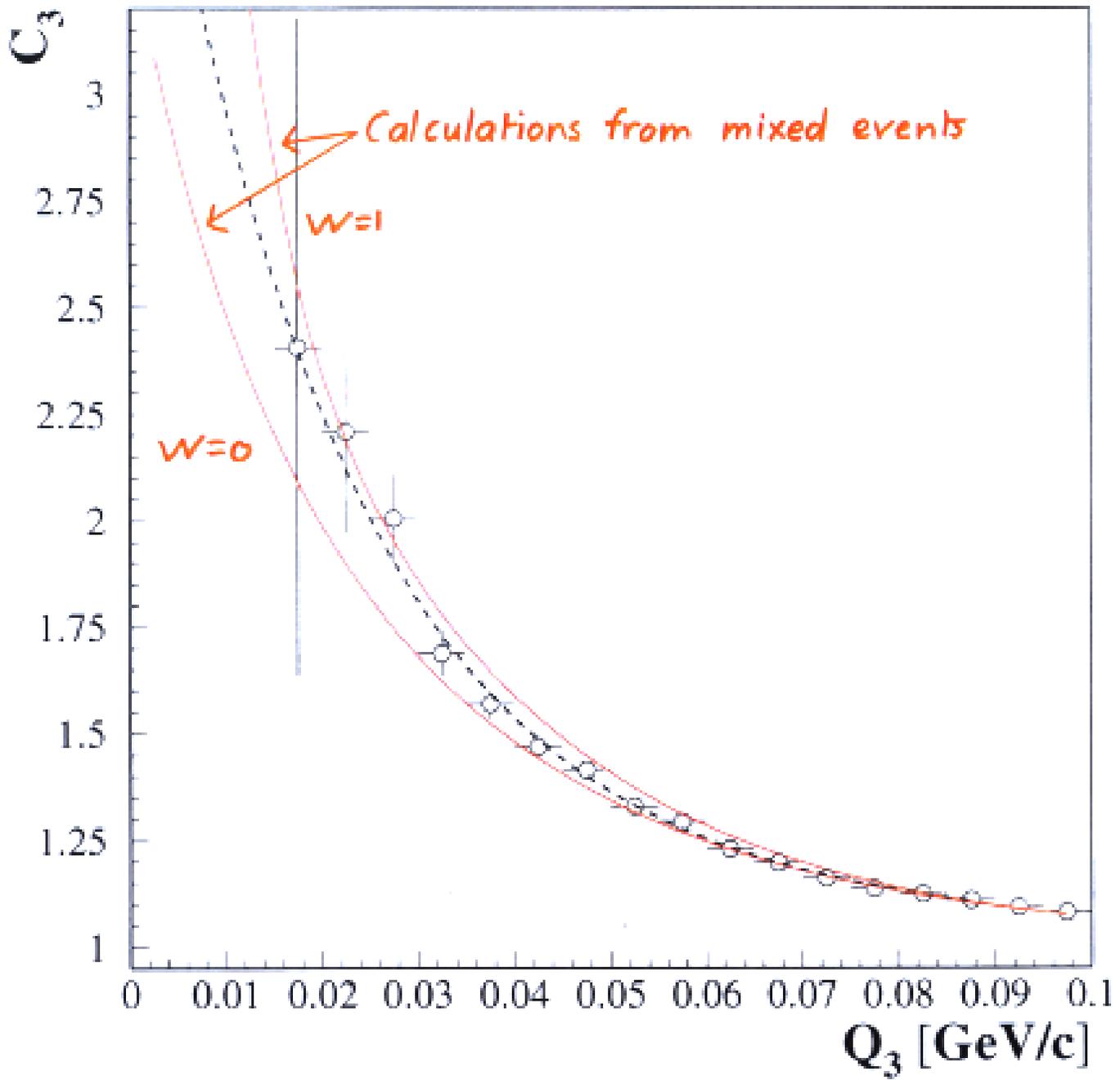
$$R_2 = 1.72 \pm 0.12$$

$$\lambda_1 = 2.79 \pm 0.32$$

$$\lambda_2 = 0.343 \pm 0.072$$

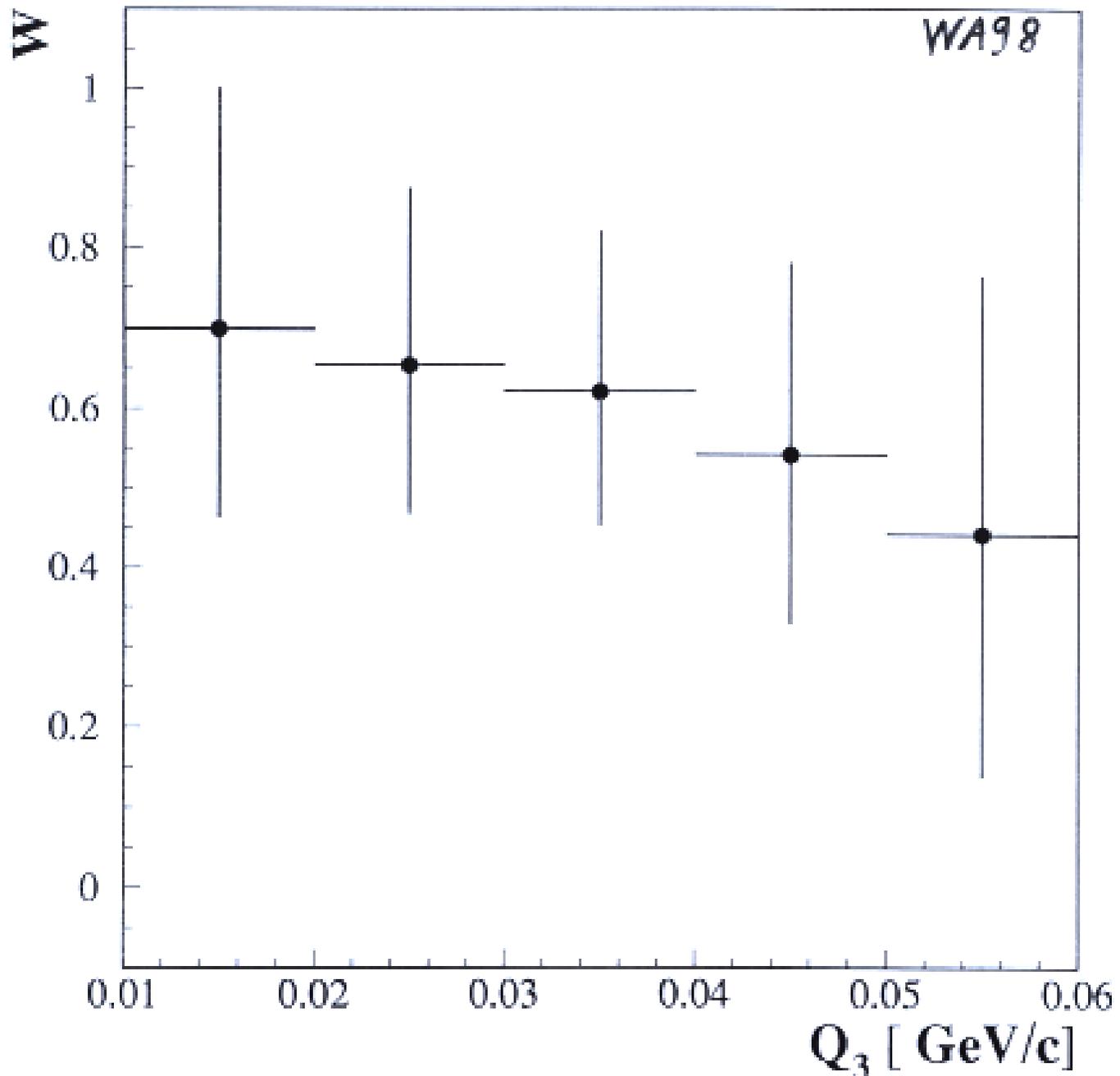
$$\chi^2 / \text{d.o.f.} = 0.88$$

$$\text{intercept at } Q_3 = 0 : 4.13 \pm 0.37 < 6$$



$$W = \frac{(C_3(Q_3) - 1) - (C_2(Q_{12}) - 1) - (C_2(Q_{23}) - 1) - (C_2(Q_{31}) - 1)}{2\sqrt{(C_2(Q_{12}) - 1)(C_2(Q_{23}) - 1)(C_2(Q_{31}) - 1)}}$$

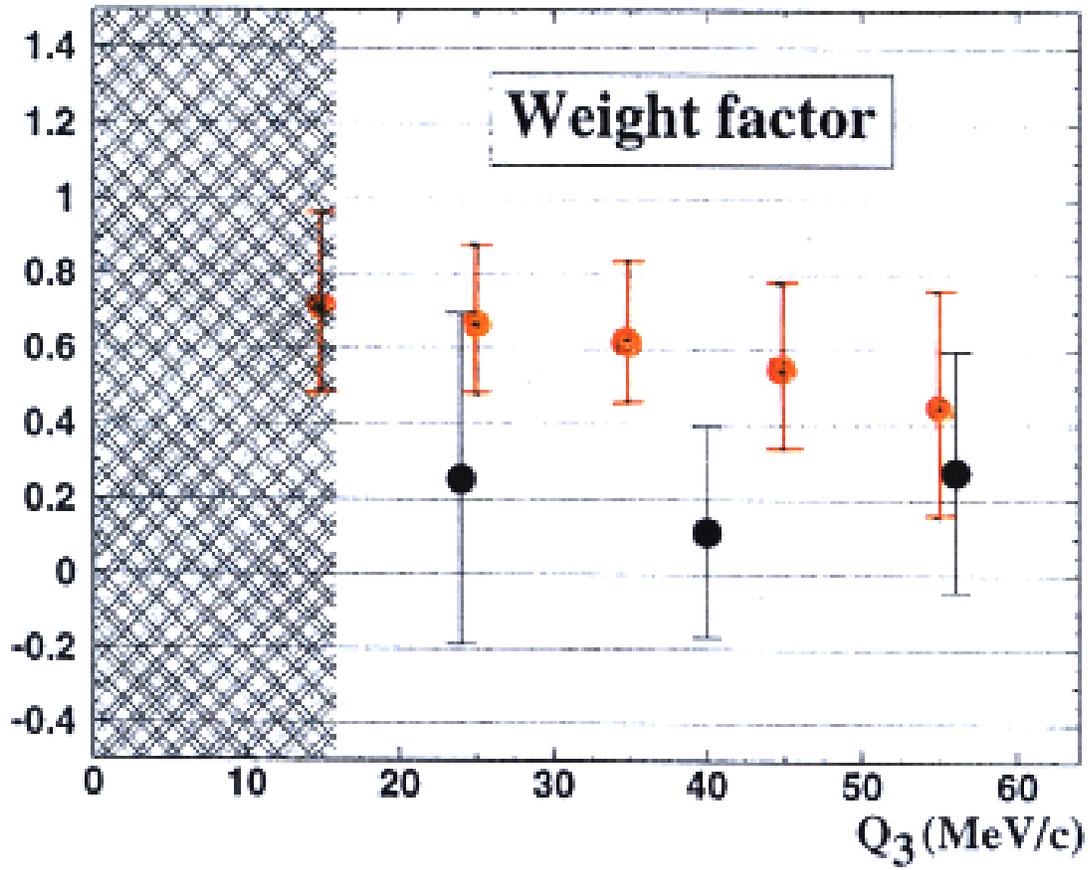
Phys. Rev. Lett. 85 (2000) 2895



statistical + systematical errors

weighted mean  $\langle W \rangle = 0.606 \pm 0.005 \pm 0.179$

W



- Lead-Lead WA98  $\pi^- \pi^- \pi^-$
- Sulphur-Lead NA44  $\pi^+ \pi^+ \pi^-$

## Summary:

$\Pi^-$  : hydrodynamical model on single distrib. (VV-H)  
favor low  $T$  and high transverse flow

$\Pi^-/\Pi^+$ : enhancement at small  $m_T$

indep. of  $Y$  between 2.2 and 3.2

$\sim$  indep. of centrality for  $b < 10$  fm

$\sim$  equal contribution from Coulomb and hyp. decays

$\Pi^-\Pi^-$ : 2 analysis of the full data as a f. of  $K_T$

- duration of emission short  $\leftrightarrow$  no long-lived intermediaries

- longitudinal expansion not strictly boost inv. phase

- " " "  $>$  lateral expansion

$\Pi^-\Pi^-\Pi^-$ : substantial contribution of the genuine 3-pion correlation, for the first time in central Pb-Pb collisions

$$\langle W \rangle = 0.606 \pm 0.005 \pm 0.179$$

larger than in S-Pb from NA44

M.M. Aggarwal,<sup>1</sup> A. Agnihotri,<sup>2</sup> Z. Ahammed,<sup>3</sup> A.L.S. Angelis,<sup>4</sup> V. Antonenko,<sup>5</sup> V. Arefiev,<sup>6</sup> V. Astakhov,<sup>5</sup> V. Avdeitchikov,<sup>5</sup> T.C. Awes,<sup>7</sup> P.V.K.S. Baba,<sup>8</sup> S.K. Badyal,<sup>8</sup> C. Barlag,<sup>9</sup> S. Bathe,<sup>9</sup> B. Baticounia,<sup>6</sup> T. Bernier,<sup>10</sup> K.B. Bhalla,<sup>2</sup> V.S. Bhatia,<sup>1</sup> C. Blume,<sup>9</sup> R. Bock,<sup>11</sup> E.-M. Böhne,<sup>9</sup> Z. Bőröcz,<sup>9</sup> D. Bucher,<sup>9</sup> A. Buijs,<sup>12</sup> H. Büsching,<sup>9</sup> L. Carlen,<sup>13</sup> V. Chalyshev,<sup>4</sup> S. Chattopadhyay,<sup>3</sup> R. Cherbachev,<sup>5</sup> T. Chujo,<sup>14</sup> A. Claussen,<sup>9</sup> A.C. Das,<sup>3</sup> M.P. Decowski,<sup>16</sup> H. Delagrangé,<sup>10</sup> V. Djordjadze,<sup>6</sup> P. Donni,<sup>4</sup> I. Doubovik,<sup>5</sup> S. Dutt,<sup>8</sup> M.R. Dutta Majumdar,<sup>3</sup> K. El Chenawi,<sup>13</sup> S. Eliseev,<sup>15</sup> K. Enosawa,<sup>14</sup> P. Foka,<sup>4</sup> S. Fokin,<sup>5</sup> M.S. Ganti,<sup>3</sup> S. Garpman,<sup>13</sup> O. Gavrishchuk,<sup>6</sup> F.J.M. Geurts,<sup>12</sup> T.K. Ghosh,<sup>15</sup> R. Glasow,<sup>9</sup> S. K. Gupta,<sup>2</sup> B. Guskov,<sup>6</sup> H. Å. Gustafsson,<sup>13</sup> H. H. Gutbrod,<sup>10</sup> R. Higuchi,<sup>14</sup> I. Hrivnacova,<sup>15</sup> M. Ippolitov,<sup>5</sup> H. Kalechofsky,<sup>4</sup> R. Kamermans,<sup>12</sup> K.-H. Kampert,<sup>9</sup> K. Karadjev,<sup>5</sup> K. Karpio,<sup>17</sup> S. Kato,<sup>14</sup> S. Kees,<sup>9</sup> C. Klein-Bösing,<sup>9</sup> S. Knoche,<sup>9</sup> B. W. Kolb,<sup>11</sup> I. Kosarev,<sup>5</sup> I. Koutcheryaev,<sup>5</sup> T. Krümpel,<sup>9</sup> A. Kugler,<sup>15</sup> P. Kulinich,<sup>18</sup> M. Kurata,<sup>14</sup> K. Kurita,<sup>14</sup> N. Kuzmin,<sup>6</sup> I. Langbein,<sup>11</sup> A. Lebedev,<sup>5</sup> Y.Y. Lee,<sup>11</sup> H. Löhner,<sup>16</sup> L. Luquin,<sup>10</sup> D.P. Mahapatra,<sup>19</sup> V. Manko,<sup>5</sup> M. Martin,<sup>4</sup> G. Martínez,<sup>10</sup> A. Maximov,<sup>6</sup> G. Mgebrichvili,<sup>5</sup> Y. Miake,<sup>14</sup> Md.F. Mir,<sup>8</sup> G.C. Mishra,<sup>19</sup> Y. Miyamoto,<sup>14</sup> B. Mohanty,<sup>19</sup> M.-J. Mora,<sup>10</sup> D. Morrison,<sup>20</sup> D. S. Mukhopadhyay,<sup>3</sup> H. Naef,<sup>4</sup> B. K. Nandi,<sup>19</sup> S. K. Nayak,<sup>10</sup> T. K. Nayak,<sup>3</sup> S. Neumaier,<sup>11</sup> A. Nianine,<sup>5</sup> V. Nikitine,<sup>6</sup> S. Nikolaev,<sup>5</sup> P. Nilsson,<sup>13</sup> S. Nishimura,<sup>14</sup> P. Nomokonov,<sup>5</sup> J. Nystrand,<sup>12</sup> F.E. Obenshain,<sup>20</sup> A. Oskarsson,<sup>13</sup> I. Otterlund,<sup>13</sup> M. Pacher,<sup>15</sup> S. Pavliouk,<sup>6</sup> T. Peitzmann,<sup>9</sup> V. Petracek,<sup>15</sup> W. Pingaud,<sup>10</sup> F. Plasil,<sup>7</sup> U. von Poblotski,<sup>9</sup> M.L. Porschke,<sup>11</sup> J. Rak,<sup>15</sup> R. Raniwala,<sup>2</sup> S. Raniwala,<sup>2</sup> V.S. Ramamurthy,<sup>19</sup> N.K. Rao,<sup>8</sup> F. Retiere,<sup>20</sup> K. Reygers,<sup>9</sup> G. Roland,<sup>18</sup> L. Rosselet,<sup>4</sup> I. Roufanov,<sup>4</sup> C. Roy,<sup>10</sup> J.M. Rubio,<sup>4</sup> H. Sako,<sup>14</sup> S.S. Sambyal,<sup>8</sup> R. Santo,<sup>9</sup> S. Sato,<sup>14</sup> H. Schlagheck,<sup>9</sup> H.-R. Schmidt,<sup>11</sup> Y. Schutz,<sup>10</sup> G. Shabratova,<sup>6</sup> T.H. Shah,<sup>8</sup> I. Sibiriak,<sup>5</sup> T. Siemiarczuk,<sup>17</sup> D. Silvermyr,<sup>13</sup> B.C. Sinha,<sup>3</sup> N. Slavine,<sup>6</sup> K. Söderström,<sup>13</sup> N. Solomey,<sup>4</sup> S.P. Sørensen,<sup>7,20</sup> P. Stankus,<sup>7</sup> G. Stefanek,<sup>17</sup> P. Steinberg,<sup>18</sup> E. Stenlund,<sup>13</sup> D. Stüken,<sup>9</sup> M. Summers,<sup>15</sup> T. Svensson,<sup>13</sup> M.D. Trivedi,<sup>3</sup> A. Tsvetkov,<sup>5</sup> L. Tykarski,<sup>17</sup> J. Urbahn,<sup>11</sup> E.C.v.d. Pijl,<sup>12</sup> N.v. Eljndhoven,<sup>12</sup> G.J.v. Nieuwenhuizen,<sup>18</sup> A. Vinogradov,<sup>5</sup> Y.P. Viyogi,<sup>3</sup> A. Vodopianov,<sup>6</sup> S. Vörös,<sup>4</sup> B. Wyslouch,<sup>16</sup> K. Yagi,<sup>14</sup> Y. Yokota,<sup>14</sup> G.R. Young<sup>7</sup>

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